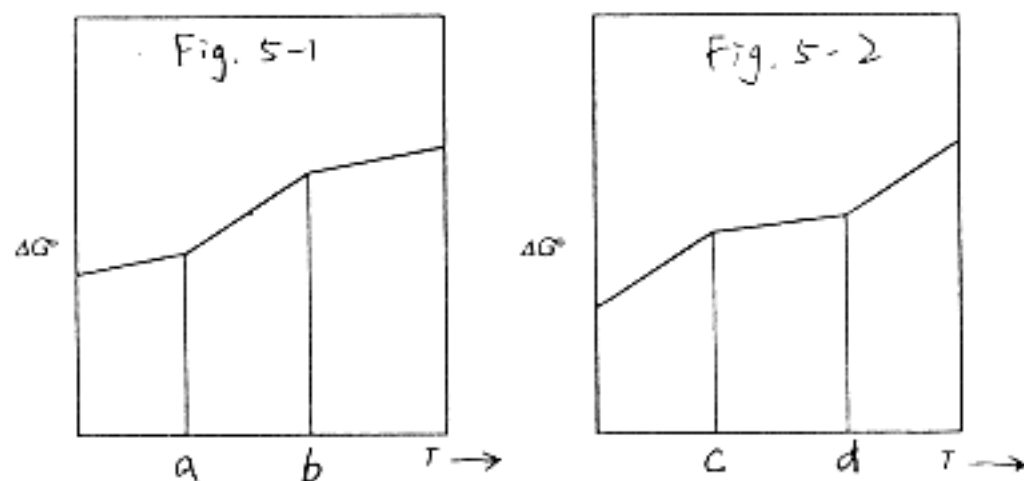
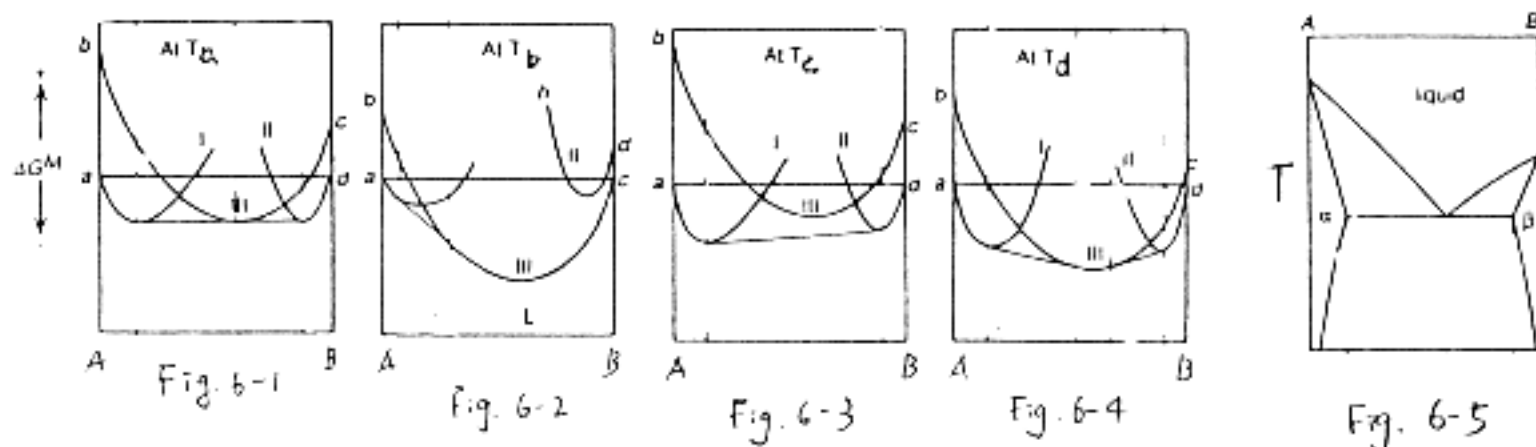


1. (12 points) Two identical bodies have constant and equal heat capacities ( $C_1=C_2=8 \text{ J/K}$ ). In addition a reversible work source is available. The initial temperatures of the two bodies are  $0^\circ\text{C}$  and  $100^\circ\text{C}$ . (a) What is the maximum work that can be delivered to the reversible work source, leaving the two bodies in thermal equilibrium? (b) What is the corresponding equilibrium temperature? (c) Is this the minimum or maximum attainable equilibrium temperature? Why?
  
2. (15 points) An adiabatic container contains 2 moles of liquid aluminum at  $700^\circ\text{C}$ . When X moles of  $\text{Cr}_2\text{O}_3$ , which is initially at  $298\text{K}$ , is added to the liquid aluminum (with which it reacts to form Cr and  $\text{Al}_2\text{O}_3$ ), the temperature of the resulting mixture of  $\text{Cr}_2\text{O}_3$ ,  $\text{Al}_2\text{O}_3$ , and Cr is raised to  $1600\text{K}$ . How do you calculate the "X"? And list all thermodynamic data required for the calculation. It is known that the melting point of Al is  $660^\circ\text{C}$  ( $=933\text{K}$ ).  $\text{Cr}_2\text{O}_3$ ,  $\text{Al}_2\text{O}_3$ , and Cr are in solid states from  $298\text{K}$  to  $1600\text{K}$ .
  
3. (10 points) One mole of monatomic ideal gas is initially at temperature of  $2000\text{K}$  and pressure of  $1 \text{ MPa}$ . The gas is cooled while the volume changes quasistatically in a process conducted so that  $PV^3=\text{constant}$ . The final temperature is  $500\text{K}$ . Determine the change in entropy of the gas.
  
4. (13 points) (a) Derive the relation  $\left(\frac{\partial P}{\partial T}\right)_S = \frac{C_p}{TV\alpha}$ , where  $\alpha = \frac{1}{V}\left(\frac{\partial V}{\partial T}\right)_P$ . (b) Ice is originally at  $-3^\circ\text{C}$  and  $1 \text{ atm}$ . The pressure is increased adiabatically until the ice reaches the melting point. How can the temperature and pressure of this melting point be calculated? What thermodynamic data do you need for the calculation?

5. (15 pt) Figures 5-1 and 5-2 show the effect of melting of the metal A and metal oxide  $AO_2$  on the Ellingham line the oxidation of the metal A. Can you identify what the melting points (for A and  $AO_2$ ) a,b,c,d representing on both figures? Also <sup>are</sup> explain reasons supporting your answer.



6. (15 pt) Figures 6-1 to 6-4 represent the molar Gibbs free energies of mixing of the system A-B at four different temperature  $T_a, T_b, T_c, T_d$ . Figure 6-5 given is the corresponding phase diagram. (1) Please redraw a phase diagram on your answer sheet and sketch the isothermal line representing  $T_a, T_b, T_c, T_d$ . (2) Draw the corresponding activities of A and B as a function of composition at temperature  $T_b$  and  $T_d$ .



Curve I :  $\alpha$  phase ; Curve II :  $\beta$  phase ; curve III : liquid phase

7. (10 pt) For the reaction

$$P_1 = 2P_2, \Delta G^\circ = 225,400 + 7.90 T \ln T - 209.4 T \text{ J}$$

- (1) What is the temperature when  $X(P_1) = X(P_2) = 0.5$  at a total pressure of 1 atm?
- (2) Use Le Chatelier's principle to predict that if the temperature is increased to 2000K, in order to keep  $X(P_1) = X(P_2) = 0.5$ , the total pressure need to be increased or decreased?
- (3) Determine the total pressure in (2), i.e. when  $T = 2000 \text{ K}$ , and  $X(P_1) = X(P_2) = 0.5$

8. (10 pt) If there is a binary solution A-B, both component A and component B obey Henry's law when the solution is dilute ( $\leq 0.10$ ). If  $P_A^\circ = 0.03 \text{ atm}$  and  $P_A = 0.04 X_A$  (in solution A-B) at 298K. If  $P_B^\circ = 0.02 \text{ atm}$  and  $P_B = 0.03 X_B$  (in solution A-B) at 298K. Calculate the partial pressure of A and B when the composition of solution are (a)  $X_A = 0.09, X_B = 0.91$  (b)  $X_B = 0.9, X_A = 0.1$  (c) When  $X_A = X_B = 0.5$ , which of the following can be the total vapor pressure, explain why? 0.01atm, 0.02atm, 0.024atm, 0.03atm, 0.04atm